NCERT Solutions for Class 7 Maths Chapter 9

Rational Numbers Class 7

Chapter 9 Rational Numbers Exercise 9.1, 9.2 Solutions

Exercise 9.1: Solutions of Questions on Page Number: 182

Q1:

List five rational numbers between:

(i) - 1 and 0 (ii) - 2 and - 1

$$\frac{-4}{5}$$
 and $\frac{-2}{3}$ (iv) $\frac{1}{2}$ and $\frac{2}{3}$

Answer:

(i) - 1 and 0

$$\frac{-1}{10}$$
, $\frac{-1}{20}$, $\frac{-1}{30}$, $\frac{-1}{40}$, $\frac{-1}{50}$

(ii) - 2 and - 1

$$-2 = \frac{-12}{6}$$
 and $-1 = \frac{-6}{6}$

Five rational numbers are

$$\frac{-11}{6}$$
, $\frac{-10}{6}$, $\frac{-9}{6}$, $\frac{-8}{6}$, $\frac{-7}{6}$

$$\frac{-4}{5}$$
 and $\frac{-2}{3}$

$$\frac{-4}{5} = \frac{-4 \times 9}{5 \times 9} = \frac{-36}{45}$$
 and $\frac{-2}{3} = \frac{-2 \times 15}{3 \times 15} = \frac{-30}{45}$

Five rational numbers are

$$\frac{-35}{45}$$
, $\frac{-34}{45}$, $\frac{-33}{45}$, $\frac{-32}{45}$, $\frac{-31}{45}$

$$\frac{1}{2}$$
 and $\frac{2}{3}$

$$\frac{1}{2} = \frac{1 \times 18}{2 \times 18} = \frac{18}{36}$$
 and $\frac{2}{3} = \frac{2 \times 12}{3 \times 12} = \frac{24}{36}$

Five rational numbers are

$$\frac{19}{36}$$
, $\frac{20}{36}$, $\frac{21}{36}$, $\frac{22}{36}$, $\frac{23}{36}$

Q2:

Write four more rational numbers in each of the following patterns:

$$\begin{array}{c} -\frac{3}{5}, \frac{-6}{10}, \frac{-9}{15}, \frac{-12}{20}, \dots \\ (ii) \end{array} \frac{-1}{4}, \frac{-2}{8}, \frac{-3}{12}, \dots \\ \frac{-1}{6}, \frac{2}{-12}, \frac{3}{-18}, \frac{4}{-24}, \dots \\ (iv) \end{array} \frac{-2}{3}, \frac{2}{-3}, \frac{4}{-6}, \frac{6}{-9}, \dots \end{array}$$

Answer

$$\frac{-3}{5}$$
, $\frac{-6}{10}$, $\frac{-9}{15}$, $\frac{-12}{20}$...
$$\frac{-3}{5}$$
, $\frac{-3 \times 2}{5 \times 2}$, $\frac{-3 \times 3}{5 \times 3}$, $\frac{-3 \times 4}{5 \times 4}$

It can be observed that the numerator is a multiple of 3 while the denominator is a multiple of 5 and as we increase them further, these multiples are increasing. Therefore, the next four rational numbers in this pattern are

$$\frac{-3\times5}{5\times5}, \frac{-3\times6}{5\times6}, \frac{-3\times7}{5\times7}, \frac{-3\times8}{5\times8}...$$

$$\frac{-15}{25}, \frac{-18}{30}, \frac{-21}{35}, \frac{-24}{40}...$$

$$\frac{-1}{4}, \frac{-2}{8}, \frac{-3}{12}...$$

$$\frac{-1}{4}, \frac{-1 \times 2}{4 \times 2}, \frac{-1 \times 3}{4 \times 3}....$$

The next four rational numbers in this pattern are

$$\frac{-1\times4}{4\times4}, \frac{-1\times5}{4\times5}, \frac{-1\times6}{4\times6}, \frac{-1\times7}{4\times7}...$$

$$\frac{-4}{16}, \frac{-5}{20}, \frac{-6}{24}, \frac{-7}{28}...$$

$$\frac{-1}{6}$$
, $\frac{2}{-12}$, $\frac{3}{-18}$, $\frac{4}{-24}$...
 $\frac{-1}{6}$, $\frac{1 \times 2}{-6 \times 2}$, $\frac{1 \times 3}{-6 \times 3}$, $\frac{1 \times 4}{-6 \times 4}$...

The next four rational numbers in this pattern are

$$\frac{1\times5}{-6\times5}, \frac{1\times6}{-6\times6}, \frac{1\times7}{-6\times7}, \frac{1\times8}{-6\times8}...$$

$$\frac{5}{-30}, \frac{6}{-36}, \frac{7}{-42}, \frac{8}{-48}...$$

$$\begin{array}{c} \frac{-2}{3}, \ \frac{2}{-3}, \frac{4}{-6}, \ \frac{6}{-9} \dots \\ \\ \frac{-2}{3}, \frac{2}{-3}, \frac{2 \times 2}{-3 \times 2}, \ \frac{2 \times 3}{-3 \times 3} \dots \end{array}$$

The next four rational numbers in this pattern are

$$\frac{2\times4}{-3\times4}, \frac{2\times5}{-3\times5}, \frac{2\times6}{-3\times6}, \frac{2\times7}{-3\times7}...$$

$$\frac{8}{-12}, \frac{10}{-15}, \frac{12}{-18}, \frac{14}{-21}...$$

Give four rational numbers equivalent to:

$$\frac{-2}{7} \frac{5}{\text{(ii)}} \frac{4}{9}$$

Answer:

$$\frac{-2}{7}$$

Four rational numbers are

$$\frac{-2 \times 2}{7 \times 2}, \frac{-2 \times 3}{7 \times 3}, \frac{-2 \times 4}{7 \times 4}, \frac{-2 \times 5}{7 \times 5}$$

$$\frac{-4}{14}, \frac{-6}{21}, \frac{-8}{28}, \frac{-10}{35}$$

Four rational numbers are

$$\frac{5 \times 2}{-3 \times 2}, \frac{5 \times 3}{-3 \times 3}, \frac{5 \times 4}{-3 \times 4}, \frac{5 \times 5}{-3 \times 5}$$

$$\frac{10}{-6}, \frac{15}{-9}, \frac{20}{-12}, \frac{25}{-15}$$

Four rational numbers are

$$\frac{4 \times 2}{9 \times 2}, \frac{4 \times 3}{9 \times 3}, \frac{4 \times 4}{9 \times 4}, \frac{4 \times 5}{9 \times 5}$$

$$\frac{8}{18}, \frac{12}{27}, \frac{16}{36}, \frac{20}{45}$$

Q4

Draw the number line and represent the following rational numbers on it:

$$\frac{3}{4}$$
 (ii) $\frac{-5}{8}$

Answer:

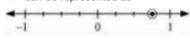
 $\frac{3}{4}$

This fraction represents 3 parts out of 4 equal parts. Therefore, each space between two integers on number line must be divided

into 4 equal parts.



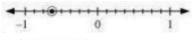
can be represented as



This fraction represents 5 parts out of 8 equal parts. Negative sign represents that it is on the negative side of number line. Therefore, each space between two integers on number line must be divided into 8 equal parts.

-5

can be represented as

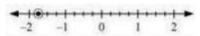


$$\frac{-7}{4} = -1\frac{3}{4}$$

This fraction represents 1 full part and 3 parts out of 4 equal parts. Negative sign represents that it is on the negative side of number line. Therefore, each space between two integers on number line must be divided into 4 equal parts.

-7

4 can be represented as



 $\frac{7}{8}$

(IV)

This fraction represents 7 parts out of 8 equal parts. Therefore, each space between two integers on number line must be divided



into 8 equal parts.

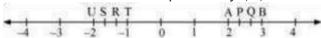


8 can be represented as

Q5 :

The points P, Q, R, S, T, U, A and B on the number line are such that,

TR = RS = SU and AP = PQ = QB. Name the rational numbers represented by P, Q, R and S.



Distance between U and T = 1 unit

It is divided into 3 equal parts.

TR = RS = SU =
$$\frac{1}{3}$$

R = $-1 - \frac{1}{3} = -\frac{3}{3} - \frac{1}{3} = \frac{-4}{3}$

S = $-1 - \frac{2}{3} = -\frac{3}{3} - \frac{2}{3} = -\frac{5}{3}$

Similarly,

AB = 1 unit

It is divided into 3 equal parts.

$$2 + \frac{1}{3} = \frac{6}{3} + \frac{1}{3} = \frac{7}{3}$$

$$2 + \frac{2}{3} = \frac{6}{3} + \frac{2}{3} = \frac{8}{3}$$

$$Q = \frac{2}{3} + \frac{2}{3} = \frac{8}{3} + \frac{2}{3} = \frac{8}{3}$$

Q6:

Which of the following pairs represent the same rational number?

$$\begin{array}{c} \frac{-7}{21} \text{and} \frac{3}{9} & \frac{-16}{20} \text{and} \frac{20}{-25} & \frac{-2}{\text{(iii)}} \frac{3}{-2} \text{and} \frac{2}{3} \\ \text{(iv)} & \frac{-3}{5} \text{and} \frac{-12}{20} & \frac{8}{-5} \text{and} \frac{-24}{15} & \frac{1}{3} \text{and} \frac{-1}{9} \\ \text{(vii)} & \frac{-5}{-9} \text{and} \frac{5}{-9} \end{array}$$

$$\frac{-7}{21}$$
 and $\frac{3}{9}$

, therefore, it does not represent same rational numbers.

$$\frac{-7}{21} = \frac{-1}{3}$$

$$\frac{3}{9} = \frac{1}{3}$$

$$\frac{-1}{3} \neq \frac{1}{3}$$

Therefore, it represents same rational numbers.

$$\frac{-16}{20}$$
 and $\frac{20}{-25}$

$$\frac{-16}{20} = \frac{-4}{5}$$

$$\frac{-20}{25} = \frac{-4}{5}$$

Therefore, it represents same rational numbers.

$$\frac{-2}{-3}$$
 and $\frac{2}{3}$

$$\frac{-2}{-3} = \frac{2}{3}$$

Therefore, it represents same rational numbers.

$$\frac{-3}{5}$$
 and $\frac{-12}{20}$

$$\frac{-12}{20} = \frac{-3}{5}$$

Therefore, it represents same rational numbers.

$$\frac{8}{-5}$$
 and $\frac{-24}{15}$

$$\frac{-24}{15} = \frac{-8}{5}$$

$$\frac{8}{-5} = \frac{-8}{5}$$

, therefore, it does not represent same rational numbers.

$$\frac{-5}{-9}$$
 and $\frac{5}{-9}$

$$\frac{1}{3}$$
 and $\frac{-1}{9}$ $\frac{-5}{-9} = \frac{5}{9}$

$$\frac{-5}{0} = \frac{5}{0}$$

$$\frac{1}{3} \neq \frac{-1}{9}$$

As $\frac{1}{3} \neq \frac{-1}{9}$ As $\frac{5}{9} \neq \frac{-5}{9}$, therefore, it does not represent same rational numbers.

Q7:

Rewrite the following rational numbers in the simplest form:

$$\frac{-8}{6}$$
 (ii) $\frac{25}{45}$

$$\frac{-44}{72}_{\text{(iv)}} \frac{-8}{10}$$

Answer:

$$\frac{-8}{6} = \frac{-4 \times 2}{3 \times 2} = \frac{-4}{3}$$

$$\frac{25}{45} = \frac{5 \times 5}{9 \times 5} = \frac{5}{9}$$

$$\frac{1}{45} = \frac{1}{9 \times 5} = \frac{1}{9}$$

$$\frac{-44}{72} = \frac{-11 \times 4}{18 \times 4} = \frac{-11}{18}$$

$$\frac{-8}{10} = \frac{-4 \times 2}{5 \times 2} = \frac{-4}{5}$$

Fill in the boxes with the correct symbol out of >, <, and =

$$\frac{-5}{7}$$
 $\square \frac{2}{3}$ $\frac{-4}{5}$ $\square \frac{-5}{7}$ $\frac{-7}{8}$ $\square \frac{14}{-16}$

$$\frac{-8}{5} \Box \frac{-7}{4} \underset{\text{(v)}}{=} \frac{1}{-3} \Box \frac{-1}{4} \underset{\text{(vi)}}{=} \frac{5}{-11} \Box \frac{-5}{11}$$

$$0 \square \frac{-7}{6}$$

$$\frac{-5}{7} = \frac{-5 \times 3}{7 \times 3} = \frac{-15}{21}$$
$$\frac{2}{3} = \frac{2 \times 7}{3 \times 7} = \frac{14}{21}$$

As - 15 < 14,

$$\frac{-5}{7} \boxed{3} \frac{2}{3}$$
 Therefore,

$$\frac{-4}{5} = \frac{-4 \times 7}{5 \times 7} = \frac{-28}{35}$$
$$\frac{-5}{7} = \frac{-5 \times 5}{7 \times 5} = \frac{-25}{35}$$

As - 28 < - 25

Therefore,
$$\frac{-4}{5} \boxed{<} \frac{-5}{7}$$

(iii) Here,
$$\frac{14}{-16} = \frac{7 \times 2}{-8 \times 2} = \frac{7}{-8} = \frac{-7}{8}$$

$$\frac{-7}{8} \boxed{=} \frac{14}{-16}$$
 Therefore,

$$\frac{-8}{5} = \frac{-8 \times 4}{5 \times 4} = \frac{-32}{20}$$
$$\frac{-7}{4} = \frac{-7 \times 5}{4 \times 5} = \frac{-35}{20}$$

As - 32 > - 35,

Therefore,
$$\frac{-8}{5}$$
 $\rightarrow \frac{-7}{4}$

$$\frac{-1}{3} = \frac{-1 \times 4}{3 \times 4} = \frac{-4}{12}$$
$$\frac{-1}{4} = \frac{-1 \times 3}{4 \times 3} = \frac{-3}{12}$$

As - 4 < - 3,

Therefore,
$$\frac{-1}{3} \le \frac{-1}{4}$$

$$\frac{5}{-11} = \frac{-5}{11}$$

$$0 \ge \frac{-7}{6}$$

Q9:

Which is greater in each of the following?

$$\frac{2}{3}, \frac{5}{2}$$
 (ii) $\frac{-5}{6}, \frac{-4}{3}$ (iii) $\frac{-3}{4}, \frac{2}{-3}$

$$\frac{-1}{4}, \frac{1}{4}_{(v)} -3\frac{2}{7}, -3\frac{4}{5}$$

Answer:

$$\frac{2}{3}, \frac{5}{2}$$

By converting these into like fractions,

$$\frac{2}{3} = \frac{2 \times 2}{3 \times 2} = \frac{4}{6}$$

$$\frac{5}{2} = \frac{5 \times 3}{2 \times 3} = \frac{15}{6}$$

As 15 > 4 therefore $\frac{5}{2}$ is greater

$$\frac{-5}{6}, \frac{-4}{3}$$

$$\frac{-4}{3} = \frac{-4 \times 2}{3 \times 2} = \frac{-8}{6}$$

As -5 > -8, therefore, $\frac{-5}{6}$ is greater.

(iii)

$$\frac{-3}{4}$$
, $\frac{2}{-3}$

Or,
$$\frac{-3}{4}$$
, $\frac{-2}{3}$

By converting these into like fractions,

$$\frac{-3}{4} = \frac{-3 \times 3}{4 \times 3} = \frac{-9}{12}$$
$$\frac{-2}{3} = \frac{-2 \times 4}{3 \times 4} = \frac{-8}{12}$$

As -8 > -9, therefore, $\frac{-2}{3}$ is greater.

$$\frac{-1}{4}, \frac{1}{4}$$

$$\frac{1}{4} > \frac{-1}{4}$$

$$-3\frac{2}{7}, -3\frac{4}{5}$$

$$\frac{-23}{7}$$
, $\frac{-19}{5}$

By converting these into like fractions,

$$\frac{-23}{7} = \frac{-23 \times 5}{7 \times 5} = \frac{-115}{35}$$
$$\frac{-19}{5} = \frac{-19 \times 7}{5 \times 7} = \frac{-133}{35}$$

As -115 > -133, therefore, $-3\frac{2}{7}$ is greater.

Q10 ·

Write the following rational numbers in ascending order:

$$\frac{-3}{5}, \frac{-2}{5}, \frac{-1}{5}$$
 (ii) $\frac{-1}{3}, \frac{-2}{9}, \frac{-4}{3}$ (iii) $\frac{-3}{7}, \frac{-3}{2}, \frac{-3}{4}$

Answer

$$\frac{-3}{5}$$
, $\frac{-2}{5}$, $\frac{-1}{5}$

$$\therefore \frac{-3}{5} < \frac{-2}{5} < \frac{-1}{5}$$

$$\frac{-1}{3}, \frac{-2}{9}, \frac{-4}{3}$$

By converting these into like fractions,

$$\frac{-1 \times 3}{3 \times 3}, \frac{-2}{9}, \frac{-4 \times 3}{3 \times 3}$$
$$\frac{-3}{9}, \frac{-2}{9}, \frac{-12}{9}$$

$$\therefore \frac{-4}{3} < \frac{-1}{3} < \frac{-2}{9}$$

$$\frac{-3}{7}, \frac{-3}{2}, \frac{-3}{4}$$

By converting these into like fractions,

$$\frac{-3\times4}{7\times4}, \frac{-3\times14}{2\times14}, \frac{-3\times7}{4\times7}$$

$$\frac{-12}{28}, \frac{-42}{28}, \frac{-21}{28}$$

$$\therefore \frac{-3}{2} < \frac{-3}{4} < \frac{-3}{7}$$

Exercise 9.2: Solutions of Questions on Page Number: 190

Q1:

Find the sum:

$$\frac{4}{5} + \left(\frac{-11}{4}\right)_{\text{(ii)}} \frac{5}{3} + \frac{3}{5}_{\text{(iii)}} \frac{-9}{10} + \frac{22}{15}$$

$$\frac{-3}{-11} + \frac{5}{9}_{\text{(v)}} \frac{-8}{19} + \frac{(-2)}{57}_{\text{(vi)}} \frac{-2}{3} + 0$$

$$-2\frac{1}{3} + 4\frac{3}{5}$$
(vii)

Answer:

$$\frac{5}{3} + \frac{3}{5}$$

L.C.M of 3 and 5 is 15.

$$\frac{5}{3} + \frac{3}{5} = \frac{5 \times 5}{3 \times 5} + \frac{3 \times 3}{5 \times 3} = \frac{25}{15} + \frac{9}{15} = \frac{25 + 9}{15} = \frac{34}{15}$$

$$\frac{-9}{10} + \frac{22}{15}$$

L.C.M of 10 and 15 is 30

$$\frac{-9}{10} + \frac{22}{15} = \frac{-9 \times 3}{10 \times 3} + \frac{22 \times 2}{15 \times 2} = \frac{-27}{30} + \frac{44}{30} = \frac{-27 + 44}{30} = \frac{17}{30}$$

$$\frac{-3}{-11} + \frac{5}{9} = \frac{3}{11} + \frac{5}{9}$$

L.C.M of 11 and 9 is 99

$$\frac{3}{11} + \frac{5}{9} = \frac{3 \times 9}{11 \times 9} + \frac{5 \times 11}{9 \times 11} = \frac{27}{99} + \frac{55}{99} = \frac{27 + 55}{99} = \frac{82}{99}$$

$$\frac{-8}{19} + \frac{(-2)}{57} = -\frac{8}{19} - \frac{2}{57}$$

L.C.M of 19 and 57 is 57.

$$-\frac{8}{19} - \frac{2}{57} = -\frac{8 \times 3}{19 \times 3} - \frac{2}{57} = -\frac{24}{57} - \frac{2}{57} = \frac{-24 - 2}{57} = \frac{-26}{57}$$

$$\frac{-2}{3} + 0 = \frac{-2}{3}$$
(vi)
$$-2\frac{1}{3} + 4\frac{3}{5} = \frac{-7}{3} + \frac{23}{5}$$

L.C.M of 3 and 5 is 15.

$$\frac{-7}{3} + \frac{23}{5} = \frac{-7 \times 5}{3 \times 5} + \frac{23 \times 3}{5 \times 3} = \frac{-35}{15} + \frac{69}{15} = \frac{-35 + 69}{15} = \frac{34}{15}$$

Q2:

Find

$$\frac{7}{24} - \frac{17}{36} \underset{\text{(ii)}}{\frac{5}{63}} - \left(\frac{-6}{21}\right) \underset{\text{(iii)}}{\frac{-6}{13}} - \left(\frac{-7}{15}\right)$$

$$\frac{-3}{8} - \frac{7}{11} \underset{\text{(v)}}{\frac{-3}{9}} - 6$$

Answer:

$$\frac{7}{24} - \frac{17}{36}$$

L.C.M of 24 and 36 is 72.

$$\frac{7}{24} - \frac{17}{36} = \frac{7 \times 3}{24 \times 3} - \frac{17 \times 2}{36 \times 2} = \frac{21}{72} - \frac{34}{72} = \frac{21 - 34}{72} = \frac{-13}{72}$$

$$\frac{5}{63} - \left(\frac{-6}{21}\right) = \frac{5}{63} + \frac{2}{7}$$
(ii)

L.C.M of 63 and 7 is 63.

$$\frac{5}{63} + \frac{2}{7} = \frac{5}{63} + \frac{2 \times 9}{7 \times 9} = \frac{5}{63} + \frac{18}{63} = \frac{5+18}{63} = \frac{23}{63}$$

$$\frac{-6}{13} - \left(\frac{-7}{15}\right) = \frac{-6}{13} + \frac{7}{15}$$
(iii)

L.C.M of 13 and 15 is 195.

$$\frac{-6}{13} + \frac{7}{15} = \frac{-6 \times 15}{13 \times 15} + \frac{7 \times 13}{15 \times 13} = \frac{-90}{195} + \frac{91}{195} = \frac{-90 + 91}{195} = \frac{1}{195}$$

$$\frac{-3}{8} - \frac{7}{11}$$
(iv)

L.C.M of 8 and 11 is 88.

$$\frac{-3}{8} - \frac{7}{11} = -\frac{3 \times 11}{8 \times 11} - \frac{7 \times 8}{11 \times 8} = -\frac{33}{88} - \frac{56}{88} = \frac{-33 - 56}{88} = \frac{-89}{88}$$

$$-2\frac{1}{9} - 6 = -\frac{19}{9} - \frac{6}{1}$$

L.C.M of 9 and 1 is 9.

$$-\frac{19}{9} - \frac{6}{1} = -\frac{19}{9} - \frac{6 \times 9}{1 \times 9} = -\frac{19}{9} - \frac{54}{9} = \frac{-19 - 54}{9} = \frac{-73}{9}$$

Q3:

Find the product:

$$\frac{9}{2} \times \left(\frac{-7}{4}\right)_{\text{(ii)}} \frac{3}{10} \times (-9)_{\text{(iii)}} \frac{-6}{5} \times \frac{9}{11}$$

$$\frac{3}{7} \times \left(\frac{-2}{5}\right)_{\text{(v)}} \frac{3}{11} \times \frac{2}{5}_{\text{(vi)}} \frac{3}{-5} \times \frac{-5}{3}$$

Answer:
$$\frac{9}{2} \times \left(\frac{-7}{4}\right) = \frac{9 \times (-7)}{2 \times 4} = \frac{-63}{8}$$

$$\frac{3}{10} \times \left(-9\right) = \frac{3}{10} \times \frac{\left(-9\right)}{1} = \frac{3 \times (-9)}{10 \times 1} = \frac{-27}{10}$$

$$\frac{3}{7} \times \left(\frac{-2}{5}\right) = \frac{3 \times (-2)}{7 \times 5} = \frac{-6}{35}$$

$$\lim_{\text{(ii)}} \frac{-6}{5} \times \frac{9}{11} = \frac{-6 \times 9}{5 \times 11} = \frac{-54}{55}$$

$$\frac{3}{11} \times \frac{2}{5} = \frac{3 \times 2}{11 \times 5} = \frac{6}{55}$$
(v)

Find the value of:

 $\frac{3}{11} \times \frac{2}{5} = \frac{3 \times 2}{11 \times 5} = \frac{6}{55}$

 $\frac{3}{-5} \times \frac{-5}{3} = \frac{3 \times (-5)}{(-5) \times 3} = \frac{-15}{-15} = 1$

$$\begin{array}{c} (-4) \div \frac{2}{3} & \frac{-3}{5} \div 2 & \frac{-4}{5} \div (-3) \\ \\ \frac{-1}{8} \div \frac{3}{4} & \frac{-2}{13} \div \frac{1}{7} & \frac{-7}{12} \div \left(\frac{-2}{13}\right) \\ \\ \frac{3}{13} \div \left(\frac{-4}{65}\right) \end{array}$$

$$-4 \div \frac{2}{3} = -4 \times \frac{3}{2} = \frac{-12}{2} = -6$$

$$\frac{-3}{5} \div 2 = \frac{-3}{5} \times \frac{1}{2} = \frac{-3 \times 1}{5 \times 2} = \frac{-3}{10}$$

$$\frac{-4}{5} \div (-3) = \frac{-4}{5} \times \frac{1}{-3} = \frac{(-4) \times 1}{5 \times (-3)} = \frac{-4}{-15} = \frac{4}{15}$$

$$\frac{-1}{8} \div \frac{3}{4} = \frac{-1}{8} \times \frac{4}{3} = \frac{-1 \times 4}{8 \times 3} = \frac{-4}{24} = -\frac{1}{6}$$

$$\frac{-2}{13} \div \frac{1}{7} = \frac{-2}{13} \times 7 = \frac{-14}{13}$$

$$\frac{-7}{12} \div \left(\frac{-2}{13}\right) = \frac{-7}{12} \times \frac{13}{-2} = \frac{(-7) \times 13}{12 \times (-2)} = \frac{-91}{-24} = \frac{91}{24}$$

$$\frac{3}{13} \div \left(\frac{-4}{65}\right) = \frac{3}{13} \times \frac{65}{-4} = \frac{3 \times 65}{13 \times \left(-4\right)} = \frac{195}{-52} = -\frac{15}{4}$$